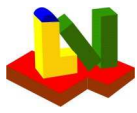


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## Layout

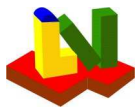
Input values:	1.234	or	1.234
Calculated values:	<b>1.234</b>	or	<b>1.234</b>
Critical values:	<b>1.234</b>	or	<b>1.234</b>
Estimated values:	<b>1.234</b>	or	<b>1.234</b>



**ASME BPVC VIII-1 2019**  
Example E4.4.7 - E4.4.8 PTB-4-2013

## Summary

[illegible]



## E4.4.7 Large End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

### Area at the wide end of a cone-cylinder-juncture without knuckle acc. App.1-8

Type of stiffener

No stiffener

External design pressure

$p_D$  14.7 psi

Hydrostatic head

$D_p$  0 psi

Calculation pressure

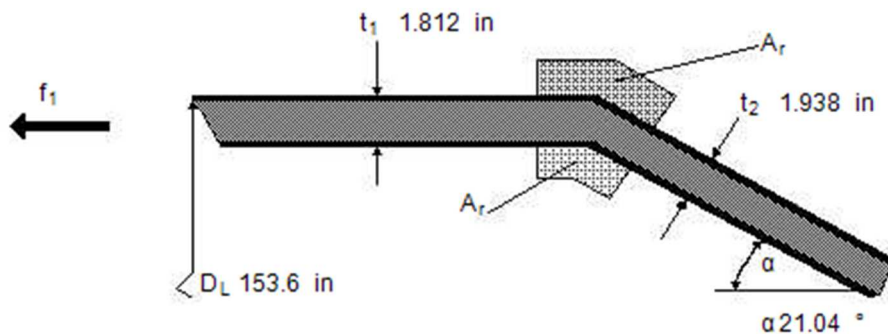
$p_0$  14.7 psi

Calculation temperature

$T_0$  300 °F

Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure

$f_1$  497.1 lbf/in



### Cylinder

Final wall thickness

$t_1$  1.812 in

Wall thickness allowance

$c_1$  0 in

Allowance (corrosion)

$c_2$  0.125 in

Final thickness without allowances

$t_s$  1.687 in

Outside diameter

$D_L$  153.6 in

Tip radius ( $=D_L/2$ )

$R_L$  76.81 in

Required thickness without allowances (UG-28)

$t_{1r}$  0.9549 in

Required thickness with allowances (UG-28)

$t_{1r+}$  1.08 in

Joint efficiency factor

$E_1$  1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

$S_s$  20015 psi

Modulus of elasticity

$E_s$  2.9e+7 psi

### Cone

Final wall thickness

$t_2$  1.938 in

Wall thickness allowance

$c_1$  0 in

Allowance (corrosion)

$c_2$  0.125 in

Final thickness without allowances

$t_c$  1.813 in

Half apex angle ( $\leq 60^\circ$ )

$\alpha$  21.04 °

Required thickness without allowances (UG-33)

$t_{2r}$  0.3639 in

Required thickness with allowances (UG-33)

$t_{2r+}$  0.4889 in

Joint efficiency factor

$E_2$  1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

$S_c$  20015 psi

Modulus of elasticity

$E_c$  2.9e+7 psi

### Stiffening ring

Material K02700-SA-516-70-Class:-Size:

Actual cross section of the stiffener

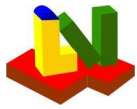
$A_r$  34 in<sup>2</sup>

Allowable stress

$S_r$  20015 psi

Modulus of elasticity

$E_r$  2.9e+7 psi



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Factor ( $\geq 1$ )  
Ratio  
Angle  
Effective load  
Cross sectional area  
Effective area

k  
 $P_0/S_s E_1$  **7.344e-4**  
 $D_{el}$  **1.836** °  
 $Q_L$  **1062** lbf/in  
 $A_{rL}$  **1.565** in<sup>2</sup>  
 $A_{eL}$  **32.14** in<sup>2</sup>

Required cross section of reinforcement

$A_{req}$  **0** in<sup>2</sup>

Remark **Stiffening required acc. App. 1-8 (b)**

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

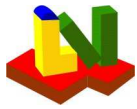
$$Q_L = P_0 \cdot \frac{R_L}{2} + f_1 = 1.014 \text{ bar} \cdot \frac{1951 \text{ mm}}{2} + 87.06 \text{ N/mm} = 185.9 \text{ N/mm}$$

$$A_{rL} = \frac{k \cdot Q_L \cdot R_L \cdot \tan(\alpha)}{S_s \cdot E_1} \cdot \left( 1 - \frac{P_0 \cdot R_L - Q_L}{4 \cdot Q_L} \cdot \frac{D_{el}}{\alpha} \right) = \quad (1)$$

$$\frac{1 \cdot 185.9 \text{ N/mm} \cdot 1951 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} \cdot \left( 1 - \frac{1.014 \text{ bar} \cdot 1951 \text{ mm} - 185.9 \text{ N/mm}}{4 \cdot 185.9 \text{ N/mm}} \cdot \frac{1.836^\circ}{21.04^\circ} \right) = 1010 \text{ mm}^2$$

$$A_{eL} = 0.55 \cdot \sqrt{(D_L \cdot t_s)} \cdot \left( \frac{t_s + t_c}{\cos(\alpha)} \right) = \quad (2)$$

$$0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} \cdot \left( \frac{42.86 \text{ mm} + 46.04 \text{ mm}}{0.9333} \right) = 20736 \text{ mm}^2$$

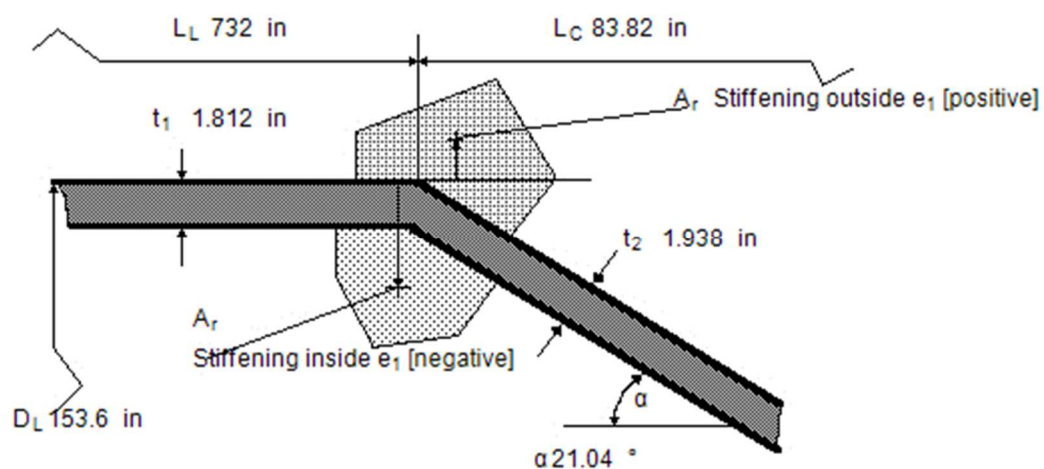


## E4.4.7 Large End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

**Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8**

**(Line-of-support)**

External design pressure	$p_D$	14.7 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	14.7 psi
Calculation temperature	$T_0$	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	$f_1$	497.1 lbf/in



**Cylinder**

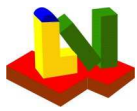
Design wall thickness	$t_1$	1.812 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Final thickness without allowances	$t_s$	1.687 in
Required thickness without allowances (UG-28)	$t_{1r}$	0.9549 in
Required thickness with allowances (UG-28)	$t_{1r+}$	1.08 in
Outside diameter	$D_L$	153.6 in
Tip radius ( $=D_L/2$ )	$R_L$	76.81 in
Buckling length	$L_L$	732 in

**Cone**

Design wall thickness	$t_2$	1.938 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Final thickness without allowances	$t_c$	1.813 in
Required thickness without allowances (UG-33)	$t_{2r}$	0.3639 in
Required thickness with allowances (UG-33)	$t_{2r+}$	0.4889 in
Half apex angle ( $\leq 60^\circ$ )	$\alpha$	21.04 °
Buckling length	$L_C$	83.82 in

**Stiffening ring**

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	$S_y$	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	$e_1$	in
Cross sectional area	$A_r$	0 in <sup>2</sup>
Moment of inertia	$I_r$	in <sup>4</sup>



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Equivalent length	M	393.8 in
Effective load	$F_L$	5980 lbf/in
Reference area	$A_{TL}$	693.6 in <sup>2</sup>
Factor	B	993.4 psi
Factor (see material chart)	A	6.96e-5
Required moment of inertia	$I_s$	81.38 in <sup>4</sup>
Required moment of inertia	$I'_s$	104.5 in <sup>4</sup>
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	8.856 in
Available moment of inertia	$I'$	in <sup>4</sup>

Remark

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1951 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{RL^2 - RS^2}{3 \cdot R_L \cdot \tan(\alpha)} =$$

$$\frac{-1951 \text{ mm} \cdot 0.3846}{2} + \frac{18593 \text{ mm}}{2} + \frac{(1951 \text{ mm})^2 - (1172 \text{ mm})^2}{3 \cdot 1951 \text{ mm} \cdot 0.3846} = 10002 \text{ mm}$$

App. 1-8 b-3) Step 1

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) =$$

$$1.014 \text{ bar} \cdot 10002 \text{ mm} + 87.06 \text{ N/mm} \cdot 0.3846 = 1047 \text{ N/mm}$$

App. 1-8 b-3) Step 1

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s =$$

$$18593 \text{ mm} \cdot \frac{42.86 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.04 \text{ mm}}{2} + 0 \text{ mm}^2 = 447474 \text{ mm}^2$$

App. 1-8 a)

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{1047 \text{ N/mm} \cdot 3902 \text{ mm}}{447474 \text{ mm}^2} = 6.849 \text{ N/mm}^2$$

App. 1-8 b-3) Step 1

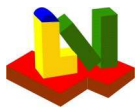
$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{14} = 3.387e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{10.9} = 4.35e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} = 224.9 \text{ mm}$$



## E4.4.7 Small End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

### Area at the small end of a cone-cylinder-juncture without knuckle

Type of stiffener

No stiffener

External design pressure

$p_D$  14.7 psi

Hydrostatic head

$D_p$  0 psi

Calculation pressure

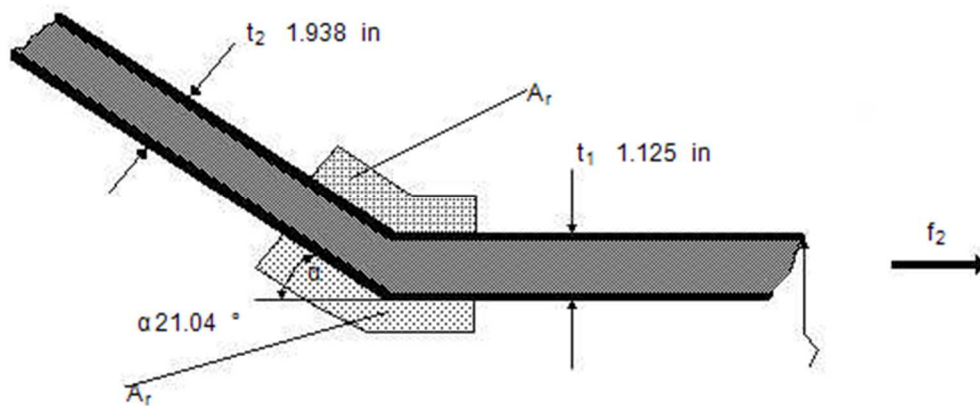
$p_0$  14.7 psi

Calculation temperature

$T_0$  300 °F

Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure

$f_2$  913 lbf/in



### Cylinder

Final wall thickness

$t_1$  1.125 in

Wall thickness allowance

$c_1$  0 in

Allowance (corrosion)

$c_2$  0.125 in

Final thickness without allowances

$t_s$  1 in

Outside diameter

$D_S$  92.25 in

Tip radius  $(=D_S/2)$

$R_S$  46.12 in

Required thickness without allowances (UG-28)

$t_{1r}$  0.6718 in

Required thickness with allowances (UG-28)

$t_{1r+}$  0.7968 in

Joint efficiency factor

$E_1$  1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

$S_s$  20015 psi

Modulus of elasticity

$E_s$  2.9e+7 psi

### Cone

Final wall thickness

$t_2$  1.938 in

Wall thickness allowance

$c_1$  0 in

Allowance (corrosion)

$c_2$  0.125 in

Final thickness without allowances

$t_c$  1.813 in

Semi aperture angle  $(\leq 60^\circ)$

$\alpha$  21.04 °

Required thickness without allowances (UG-33)

$t_{2r}$  0.3639 in

Required thickness with allowances (UG-33)

$t_{2r+}$  0.4889 in

Joint efficiency factor

$E_2$  1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

$S_c$  20015 psi

Modulus of elasticity

$E_c$  2.9e+7 psi

### Stiffening ring

Material

Actual cross section of the stiffener

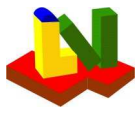
$A_r$  in<sup>2</sup>

Allowable stress

$S_r$  psi

Modulus of elasticity

$E_r$  psi



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Factor	k	1 ≥ 1
Effective load	Q <sub>S</sub>	1252 lbf/in
Cross sectional area	A <sub>rS</sub>	1.11 in <sup>2</sup>
Effective area	A <sub>eS</sub>	9.936 in <sup>2</sup>
Required cross section of the stiffener	A <sub>req</sub>	0 in <sup>2</sup>
Remark		

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

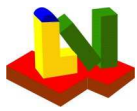
$$Q_S = P_0 \cdot \frac{R_S}{2} + f_2 = 1.014 \text{ bar} \cdot \frac{1172 \text{ mm}}{2} + 159.9 \text{ N/mm} = 219.3 \text{ N/mm}$$

$$A_{rS} = \frac{k \cdot Q_S \cdot R_S \cdot \tan(\alpha)}{S_s \cdot E_1} = \frac{1 \cdot 219.3 \text{ N/mm} \cdot 1172 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} = 716 \text{ mm}^2 \quad (3)$$

$$A_{eS} = 0.55 \cdot \sqrt{D_S \cdot t_s} \cdot \left[ \frac{t_s - t + (t_c - t_r)}{\cos(\alpha)} \right] = \quad (4)$$

$$0.55 \cdot \sqrt{2343 \text{ mm} \cdot 25.4 \text{ mm}} \cdot \left[ \frac{25.4 \text{ mm} - 17.06 \text{ mm} + (46.05 \text{ mm} - 9.242 \text{ mm})}{0.9333} \right] = 6410 \text{ mm}^2$$



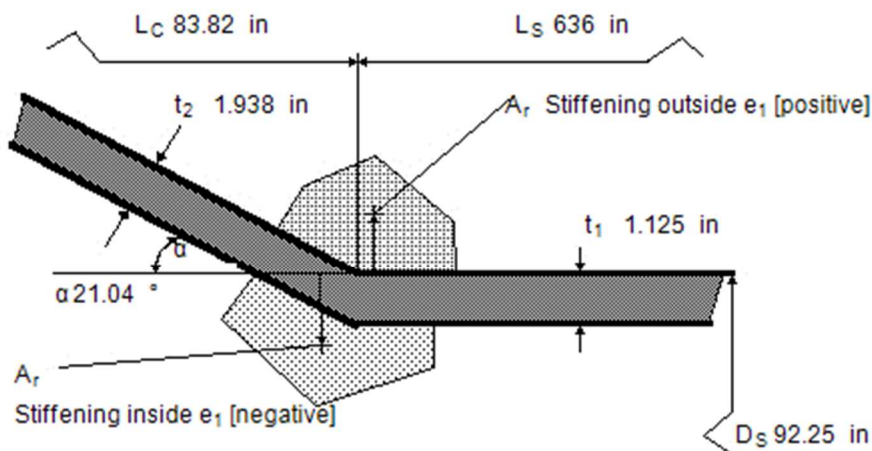


## E4.4.7 Small End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

**Moment of inertia at the small end of a cone-cylinder-juncture under external pressure acc. App.1-8**

**(Line-of-support)**

External design pressure	$p_D$	14.7 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	14.7 psi
Calculation temperature	$T_0$	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	$f_2$	913 lbf/in



**Cylinder**

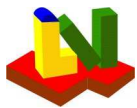
Final wall thickness	$t_1$	1.125 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Final thickness without allowances	$t_s$	1 in
Required thickness without allowances (UG-28)	$t_{1r}$	0.6718 in
Required thickness with allowances (UG-28)	$t_{1r+}$	0.7968 in
Outside diameter	$D_S$	92.25 in
Tip radius ( $=D_S/2$ )	$R_S$	46.12 in
Buckling length	$L_S$	636 in

**Cone**

Final wall thickness	$t_2$	1.938 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0.125 in
Final thickness without allowances	$t_c$	1.813 in
Required thickness without allowances (UG-33)	$t_{2r}$	0.3639 in
Required thickness with allowances (UG-33)	$t_{2r+}$	0.4889 in
Semi-apex angle ( $\leq 60^\circ$ )	$\alpha$	21.04 °
Buckling length	$L_C$	83.82 in

**Stiffening ring**

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	$S_y$	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	$e_1$	in
Cross sectional area	$A_r$	0 in <sup>2</sup>
Moment of inertia	$I_r$	in <sup>4</sup>



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Equivalent length	N	362.3 in
Effective load	$F_S$	5677 lbf/in
Reference area	$A_{TS}$	394 in <sup>2</sup>
Factor	B	997 psi
Factor (see material chart)	A	6.998e-5
Required moment of inertia	$I_s$	16.76 in <sup>4</sup>
Required moment of inertia	$I'_s$	21.53 in <sup>4</sup>
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	5.283 in
Available moment of inertia	$I'$	in <sup>4</sup>

Remark

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_S = R_L - L_C \cdot \sin(\alpha) = 1952 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$N = \frac{R_S \cdot \tan(\alpha)}{2} + \frac{L_S}{2} + \frac{RL^2 - RS^2}{6 \cdot R_S \cdot \tan(\alpha)} =$$

$$\frac{1172 \text{ mm} \cdot 0.3846}{2} + \frac{16154 \text{ mm}}{2} + \frac{(1952 \text{ mm})^2 - (1172 \text{ mm})^2}{6 \cdot 1172 \text{ mm} \cdot 0.3846} = 9203 \text{ mm}$$

$$994.3 \text{ N/mm} = 1.014 \text{ bar} \cdot 9203 \text{ mm} + 159.9 \text{ N/mm} \cdot 0.3846$$

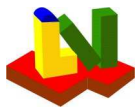
$$A_{TS} = L_S \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_S = 16154 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.05 \text{ mm}}{2} + 0 \text{ mm}^2 = 254182 \text{ mm}^2$$

$$B = \frac{3}{4} \cdot \frac{F_S \cdot D_S}{A_{TS}} = \frac{3}{4} \cdot \frac{994.3 \text{ N/mm} \cdot 2343 \text{ mm}}{254182 \text{ mm}^2} = 6.874 \text{ N/mm}^2$$

$$I_s = \frac{A \cdot DS^2 \cdot A_{TS}}{14} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{14} = 6975754 \text{ mm}^4$$

$$I'_s = \frac{A \cdot DS^2 \cdot A_{TS}}{10.9} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{10.9} = 8959684 \text{ mm}^4$$

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(D \cdot 25.4 \text{ mm})} = 134.2 \text{ mm}$$



### E4.4.8 Large and Small End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

#### Conical shells under external pressure acc. UG-33(f)

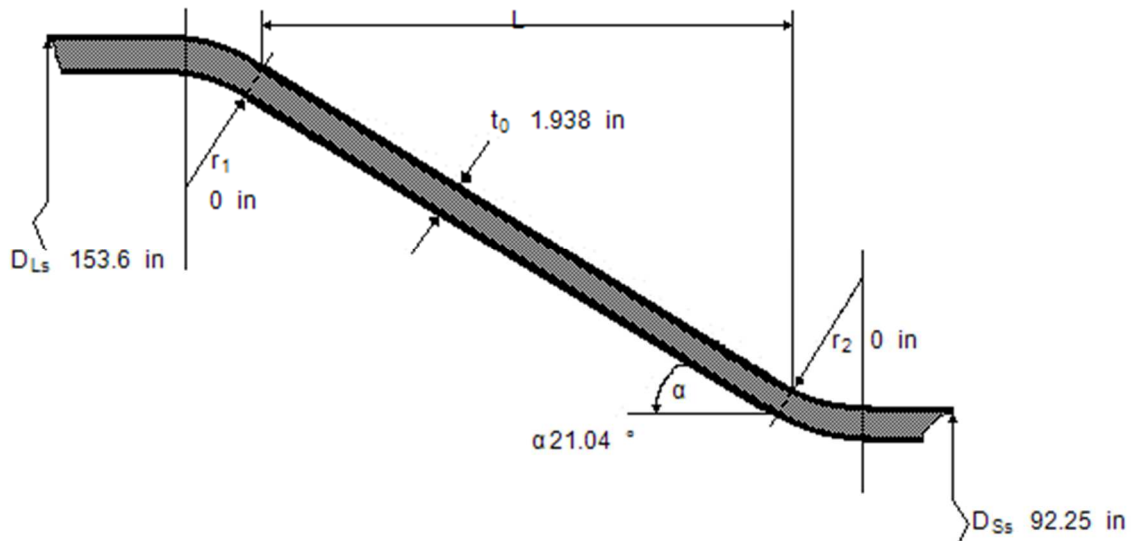
External design pressure  
Hydrostatic head  
Calculation pressure  
Calculation temperature

$p_D$  14.7 psi  
 $D_p$  0 psi  
 $p_0$  **14.7** psi  
 $T_0$  300 °F

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield  
Allowable stress  
Applicable material chart  
Modulus of elasticity

$S_y$  37710 psi  
 $S_0$  20015 psi  
Fig CS-2  
 $E$  2.9e+7 psi



Cone wall thickness with allowances  
Wall thickness allowance  
Allowance (corrosion)  
Cone wall thickness without allowances

$t_0$  1.938 in  
 $c_1$  0 in  
 $c_2$  0.125 in  
 $t$  **1.813** in

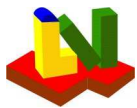
Is a cylinder connected, which does not act as line of support?

N (Y/N)

Outside diameter (wide end)  
Knuckle radius (wide end)  
Outside diameter (small end)  
Knuckle radius (small end)  
Half apex angle ( $\leq 60^\circ$ )

$D_{Ls}$  153.6 in  
 $r_1$  0 in  
 $D_{Ss}$  92.25 in  
 $r_2$  0 in  
 $\alpha$  21.04 °

**Proof for cross-section area according to App. 1-8 required for cone-connection without knuckle**



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	$t_e$	<b>1.692</b> in
Axial length of the cone		$L$	<b>79.79</b> in
Design length		$L_e$	<b>63.85</b> in
Ratio		$L_e/D_L$	<b>0.4156</b>
Ratio		$D_L/t_e$	<b>90.81</b>
Factor according to fig. 5-UGO-28.0		$A$	<b>0.004054</b>
Factor (see material chart)		$B$	<b>16850</b> psi
Factor	$2 \cdot \min(S_0, 9 \cdot B)$	$S$	<b>31589</b> psi
Allowable external pressure	( for $t_0$ )	$P$	<b>247.4</b> psi
Allowable pressure without hydrostatic head		MEP	<b>247.4</b> psi
Required thickness	( for $P_0$ )	$t$	<b>0.3664</b> in
Required thickness incl. allowances		$t+c_1+c_2$	<b>0.4914</b> in

Remark

### Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3902 \text{ mm} - 0 \text{ mm} \cdot (1 - 0.9333) = 3902 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 2343 \text{ mm} + 0 \text{ mm} \cdot (1 - 0.9333) = 2343 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3902 \text{ mm} - 2343 \text{ mm})}{2} \cdot 0.3846 = 2027 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.359 = 0 \text{ mm}$$

$$L_2 = r_2 \cdot \left( \frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.6005 \cdot 0.359 = 0 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{2027 \text{ mm}}{2} \cdot \frac{(3902 \text{ mm} + 2343 \text{ mm})}{3902 \text{ mm}} = 1622 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 0 \text{ mm} + 0 \text{ mm} + 1622 \text{ mm} = 1622 \text{ mm}$$

1) for  $D_L/t_0 \geq 10$

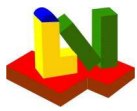
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{4 \cdot 116.2 \text{ N/mm}^2}{3 \cdot 90.81} = 1.706 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left( \frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.004054 \cdot 199948 \text{ N/mm}^2}{3 \cdot 90.81} = 5.951 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for  $D_L/t_0 < 10$



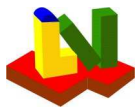
**ASME BPVC VIII-1 2019**  
Example E4.4.7 - E4.4.8 PTB-4-2013

$$P_{a1} = \left[ \frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[ \frac{2.167}{90.81} - 0.0833 \right] \cdot 116.2 \text{ N/mm}^2 = -6.905 \text{ N/mm}^2$$

UG-33 f-b) Step 2

$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[ 1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \cdot \left[ 1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \right] = 4.744 \text{ N/mm}^2$$

UG-33 f-b) Step 3

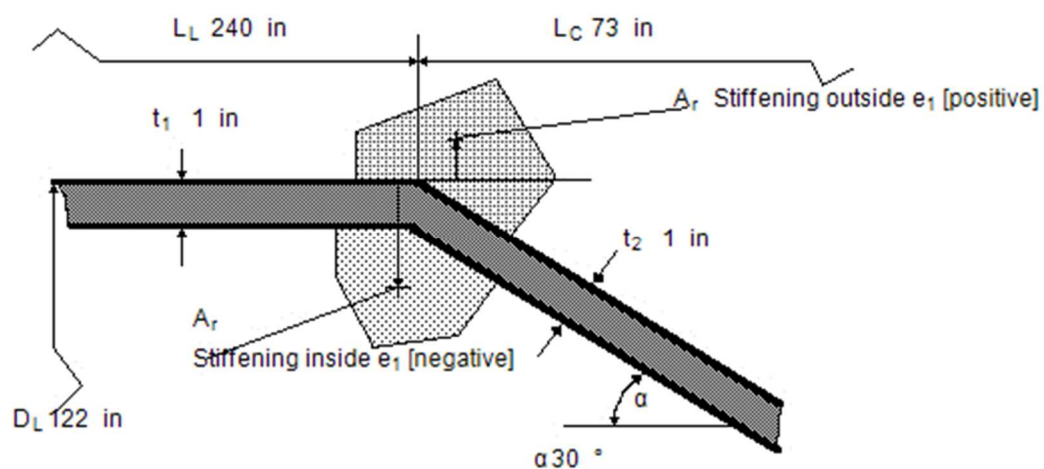


## E4.4.8 Large End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2019

**Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8**

**(Line-of-support)**

External design pressure	$p_D$	14.7 psi
Hydrostatic head	$D_p$	0 psi
Calculation pressure	$p_0$	14.7 psi
Calculation temperature	$T_0$	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	$f_1$	145 lbf/in



**Cylinder**

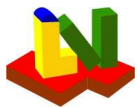
Design wall thickness	$t_1$	1 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0 in
Final thickness without allowances	$t_s$	1 in
Required thickness without allowances (UG-28)	$t_{1r}$	0.5205 in
Required thickness with allowances (UG-28)	$t_{1r+}$	0.5205 in
Outside diameter	$D_L$	122 in
Tip radius ( $=D_L/2$ )	$R_L$	61 in
Buckling length	$L_L$	240 in

**Cone**

Design wall thickness	$t_2$	1 in
Wall thickness allowance	$c_1$	0 in
Allowance (corrosion)	$c_2$	0 in
Final thickness without allowances	$t_c$	1 in
Required thickness without allowances (UG-33)	$t_{2r}$	0.3358 in
Required thickness with allowances (UG-33)	$t_{2r+}$	0.3358 in
Half apex angle ( $\leq 60^\circ$ )	$\alpha$	30 °
Buckling length	$L_C$	73 in

**Stiffening ring**

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	$S_y$	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	$e_1$	0 in
Cross sectional area	$A_r$	0 in <sup>2</sup>
Moment of inertia	$I_r$	0 in <sup>4</sup>



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Results

Equivalent length	M	134.7 in
Effective load	$F_L$	2064 lbf/in
Reference area	$A_{TL}$	156.5 in <sup>2</sup>
Factor	B	1207 psi
Factor (see material chart)	A	8.447e-5
Required moment of inertia	$I_s$	14.06 in <sup>4</sup>
Required moment of inertia	$I'_s$	18.05 in <sup>4</sup>
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	6.075 in
Available moment of inertia	$I'$	18.15 in <sup>4</sup>
Remark	Stiffening required	

### Equations

$$\cos(\alpha) = \cos(30^\circ) = 0.866$$

$$\sin(\alpha) = \sin(30^\circ) = 0.5$$

$$\tan(\alpha) = \tan(30^\circ) = 0.5774$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1549 \text{ mm} - 1854 \text{ mm} \cdot 0.5 = 445 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{RL^2 - RS^2}{3 \cdot R_L \cdot \tan(\alpha)} =$$

$$\frac{-1549 \text{ mm} \cdot 0.5774}{2} + \frac{6096 \text{ mm}}{2} + \frac{(1549 \text{ mm})^2 - (445 \text{ mm})^2}{3 \cdot 1549 \text{ mm} \cdot 0.5774} = 3421 \text{ mm}$$

App. 1-8 b-3) Step 1

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) =$$

$$1.014 \text{ bar} \cdot 3421 \text{ mm} + 25.39 \text{ N/mm} \cdot 0.5774 = 361.4 \text{ N/mm}$$

App. 1-8 b-3) Step 1

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s =$$

$$6096 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 1854 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 0 \text{ mm}^2 = 100968 \text{ mm}^2$$

App. 1-8 a)

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{361.4 \text{ N/mm} \cdot 3099 \text{ mm}}{100968 \text{ mm}^2} = 8.32 \text{ N/mm}^2$$

App. 1-8 b-3) Step 1

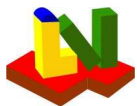
$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 8.447e-5 \cdot (3099 \text{ mm})^2 \cdot \frac{100968 \text{ mm}^2}{14} = 5850143 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 8.447e-5 \cdot (3099 \text{ mm})^2 \cdot \frac{100968 \text{ mm}^2}{10.9} = 7513945 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3099 \text{ mm} \cdot 25.4 \text{ mm})} = 154.3 \text{ mm}$$



# ASME BPVC VIII-1 2019

## Example E4.4.7 - E4.4.8 PTB-4-2013

### Appendix: Material documentation

Section 5: Zylinder/E4.4.7 Large End  
 Section 5: Kegel/E4.4.7 Large End  
 Section 5: Verstärkung/E4.4.7 Large End  
 Section 4: Verstärkung/E4.4.7 Large End/Line-of-support  
 Section 2: Zylinder/E4.4.7 Small End  
 Section 2: Kegel/E4.4.7 Small End  
 Section 7: Verstärkung/E4.4.7 Small End/Line-of-support  
 Section 1: Boden/E4.4.8 Large and Small End  
 Section 10: Verstärkung/E4.4.8 Large End/Line-of-support

#### Material specification:

Material code: K02700-SA-516-70-Class:-Size:	Regulation: ASME II.D Table 1A:2017	Spec. No.: SA-516
Short name: Carbon steel	Product: Plate	
Delivery condition:		

#### Design conditions and dimensions:

Temperature [°C]: 148.89	Thickness [mm]: 46.04
Pressure [bar]: 1.01	Outside diameter [mm]: 3902.08

#### Material values for test and design conditions:

	Test condition	Operating condition
Nominal design strength [N/mm²]:	138	138
Safety factor:	1	1
Allowable stress [N/mm²]:	138	138
Modulus of elasticity [kN/mm²]:	202.4	195.1

#### Notes:

G10: General Requirements

Upon prolonged exposure to temperatures above 425°C, the carbide phase of carbon steel may be converted to graphite. See Nonmandatory Appendix A, A-201 and A-202.

S1: Size Requirements

For Section I applications, stress values at temperatures of 450°C and above are permissible but, except for tubular products 75 mm O.D. or less enclosed within the boiler setting, use of these materials at these temperatures is not current practice.

T2: Time-Dependent Properties

Allowable stresses for temperatures of 400°C and above are values obtained from time-dependent properties.

#### Strength values at 20°C

R <sub>eH</sub>	density	Tensile strength
.	.	R <sub>m</sub> , min
N/mm²	kg/dm³	N/mm²
260	7.85	485

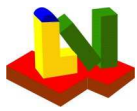
#### Strength values as a function of temperature

T	°C	40	100	150	250	325	375	425	475	525
K	N/mm²	138	138	138	138	132	123	83.8	51	21.3

#### Young's modulus-values in dependence of the temperature

T	°C	-200	-125	-75	25	100	150	200	250	300	350	400	450	500	550
E	kN/mm²	216	212	209	202	198	195	192	189	185	179	171	162	151	137





**ASME BPVC VIII-1 2019**  
Example E4.4.7 - E4.4.8 PTB-4-2013

**Mean coefficient of thermal expansion-values in dependence of the temperature**

T	°C	20	100	200	300	400	500	600	700	800
$\alpha_m$	1e-6/K	11.5	12.1	12.7	13.3	13.8	14.4	14.8	15.1	15.4

**Differential coefficient of thermal expansion-values in dependence of the temperature**

T	°C	20	100	200	300	400	500	600	700	800
$\alpha_{diff}$	1e-6/K	11.5	12.7	13.8	14.9	15.9	16.7	17.0	17.1	17.7

**Design conditions and dimensions:**

Temperature [°C]: 148.89	Thickness [mm]: 49.21
Pressure [bar]: 1.01	Outside diameter [mm]: 3902.08

**Design conditions and dimensions:**

Temperature [°C]: 148.89	Thickness [mm]: 49.23
Pressure [bar]: 1.01	Outside diameter [mm]: 2343.15